

# Introduction to Dynamic Analysis

# Static Analysis versus Dynamic Analysis

- **Static Analysis** -- the static examination of a product or a representation of the product for the purpose of inferring properties or characteristics
- **Dynamic Analysis** -- the "execution" of a product or representation of a product for the purpose of inferring properties or characteristics
- **Testing** -- the (systematic) selection and subsequent "execution" of sample inputs from a product's input space in order to infer information about the product's behavior.
  - usually trying to uncover failures
  - the most common form of dynamic analysis

# Approaches

- **Dynamic Analysis**
  - Assertions
  - Error seeding, mutation testing
  - Coverage criteria
  - Fault-based testing
  - Specification-based testing
  - Object oriented testing
  - Regression testing
- **Static Analysis**
  - Inspections
  - Software metrics
  - Symbolic execution
  - Dependence Analysis
  - Data flow analysis
  - Software Verification

# Types of Testing--what is tested

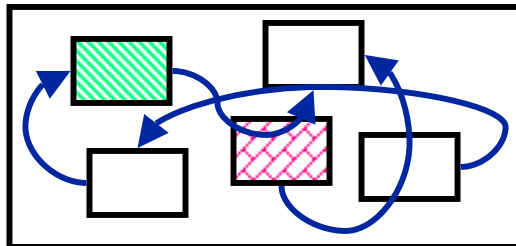
- **Unit testing**-exercise a single simple component
  - Procedure
  - Class
- **Integration testing**-exercise a collection of inter-dependent components
  - Focus on interfaces between components
- **System testing**-exercise a complete, stand-alone system
- **Acceptance testing**-customer's evaluation of a system
  - Usually a form of system testing
- **Regression testing**-exercise a changed system
  - Focus on modifications or their impact

# Approaches to testing

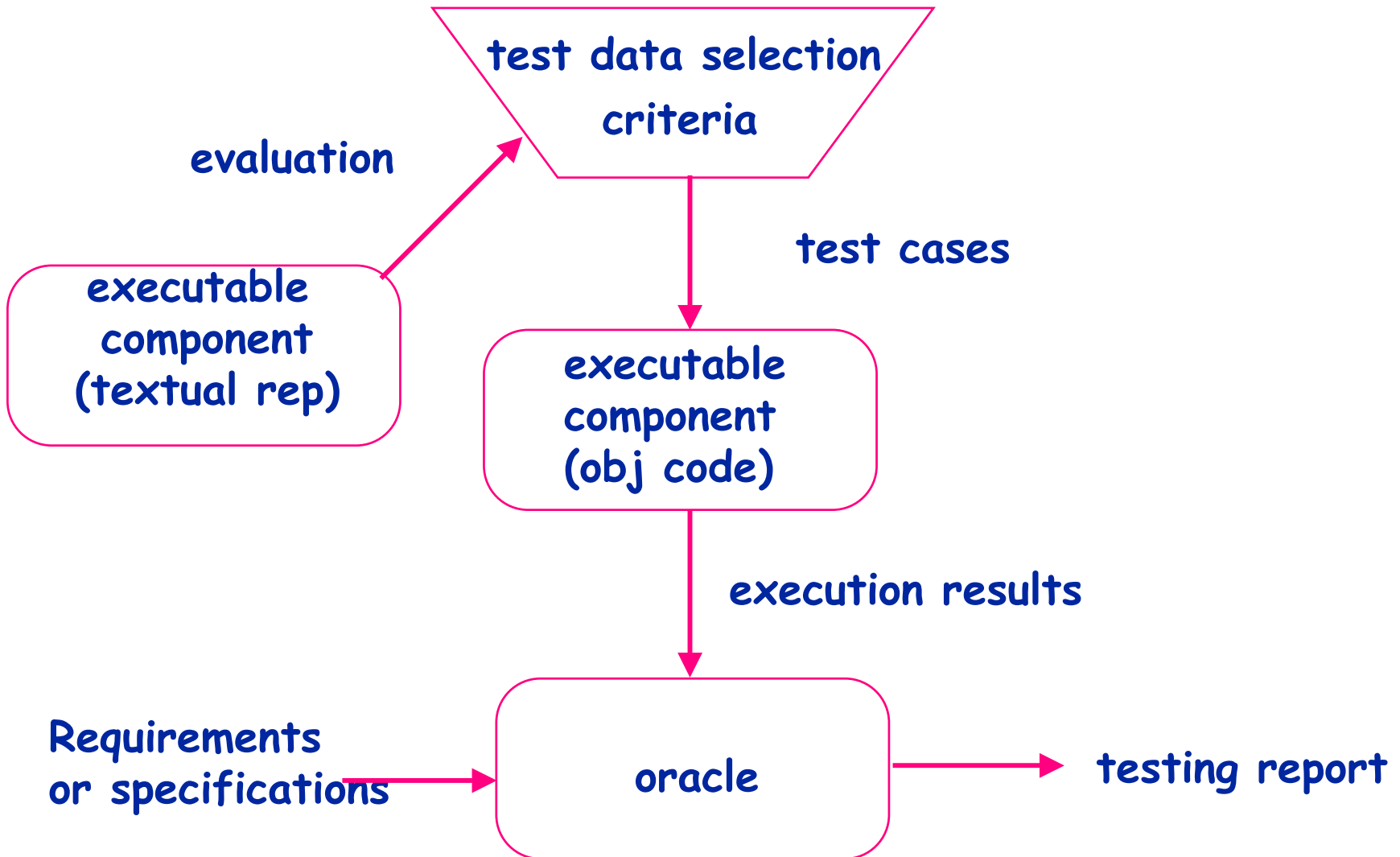
- **Black Box/Functional/Requirements based**



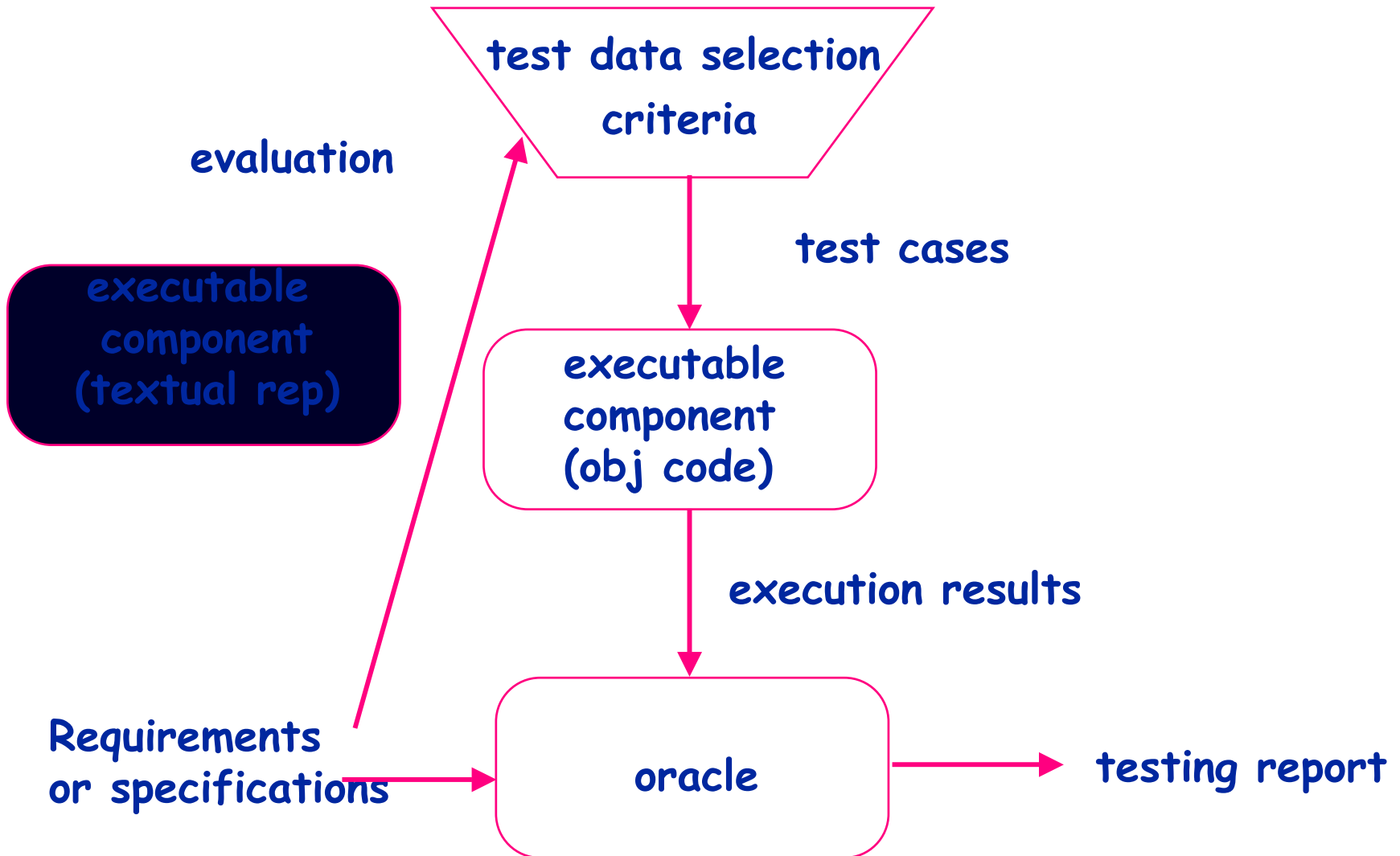
- **White Box/Structural/Implementation based**



# White box testing process



# Black box testing process



# Why black AND white box?

- **Black box**
  - May not have access to the source code
  - Often do not care how s/w is implemented, only how it performs
- **White box**
  - Want to take advantage of all the information
  - Looking inside indicates structure=> helps determine weaknesses



## Test Selection Criteria

- How do we determine what are good test cases?
- How do we know when to stop testing?

Test Adequacy

# Test Selection Criteria

- A test set  $T$  is a finite set of inputs (test cases) to an executable component
- Let  $D(S)$  be the domain of execution for program/component/system  $S$
- Let  $S(T)$  be the results of executing  $S$  on  $T$
- A test selection criterion  $C(T, S)$  is a predicate that specifies whether a test set  $T$  satisfies some selection criterion for an executable component  $S$ .
- Thus, the test set  $T$  that satisfies the Criterion  $C$  is defined as:

$$\{ t \in T \mid T \subseteq D(S) \text{ and } C(T, S) \}$$

## Ideal Test Criterion

- A test criterion is **ideal** if for any executable system  $S$  and every  $T \subseteq D(S)$  such that  $C(T, S)$ , if  $S(T)$  is correct, then  $S$  is correct
  - of course we want  $T \ll D(S)$
  - In general,  $T = D(S)$  is the only test criterion that satisfies ideal

## In general, there is no ideal test criterion

“Testing shows the presence, not the absence of bugs”  
E. Dijkstra

- Dijkstra was arguing that verification was better than testing
- But verification has similar problems
  - can't prove an arbitrary program is correct
    - can't solve the halting problem
  - can't determine if the specification is complete
- Need to use dynamic and static techniques that compliment each another

## Effectiveness a more reasonable goal

- A test criterion  $C$  is *effective* if for any executable system  $S$  and every  $T \subseteq D(S)$  such that  $C(T, S)$ ,
  - ⇒ if  $S(T)$  is correct, then  $S$  is highly reliable
  - OR
  - ⇒ if  $S(T)$  is correct, then  $S$  is guaranteed (or is highly likely) not to contain any faults of a particular type
- Currently can not do either of these very well
  - Some techniques (static and dynamic) can provide some guarantees

## Two Uses for Testing Criteria

- **Stopping rule**--when has a system been tested enough
- **Test data evaluation rule**--evaluates the quality of the selected test data
  - May use more than one criterion
  - May use different criteria for different types of testing
    - regression testing versus acceptance testing

## Black Box/Functional Test Data Selection

- Typical cases
- Boundary conditions/values
- Exceptional conditions
- Illegal conditions (if robust)
- Fault-revealing cases
  - based on intuition about what is likely to break the system
- Other special cases

## Functional Test Data Selection

- **Stress testing**
  - large amounts of data
  - worse case operating conditions
- **Performance testing**
- **Combinations of events**
  - select those cases that appear to be more error-prone
  - Select 1 way, 2 way, ... n way combinations



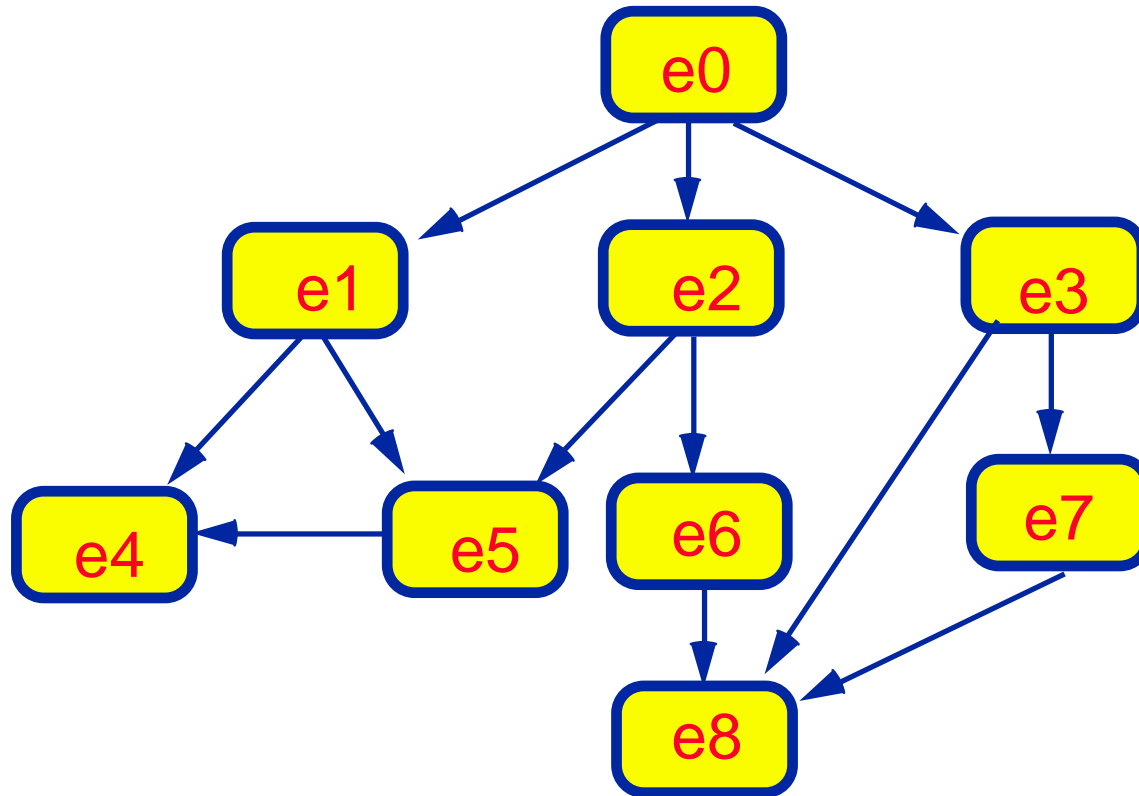
## Sequences of events

- **Common representations for selecting sequences of events**
  - Decision tables
  - Cause and effect graphs
  - Usage scenarios

# Decision Table

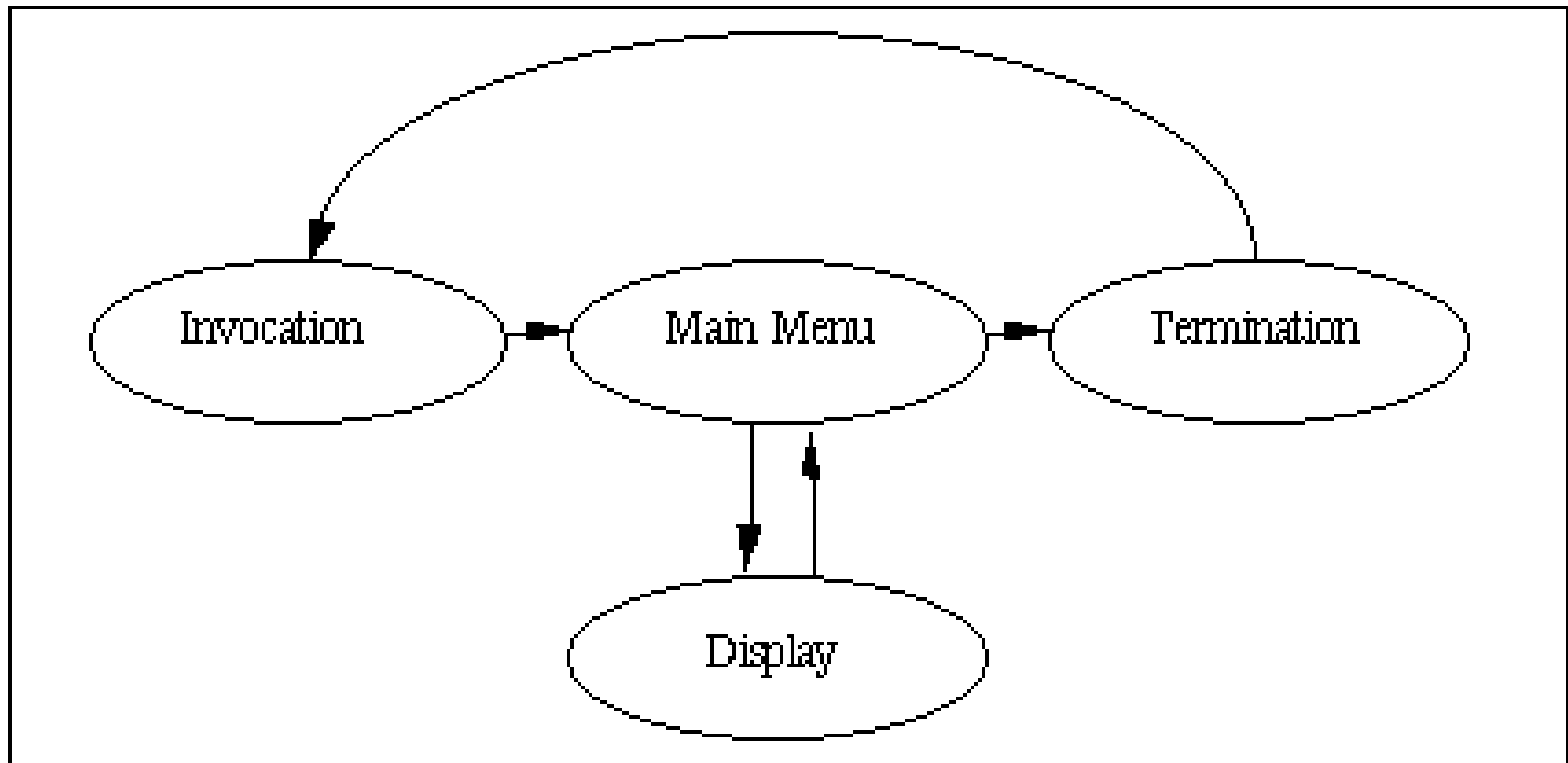
events	t1	t2	t3	t5	t6	t7	...
e1	x	x	x		-		
e2		x	x	x	x		x
e3	x			x		x	
e4	-		x		x		x
...		x			x	x	-

# Cause and Effect Graph



# Usage Scenarios

Graphical Usage Model of a Simple System



# Overview of Dynamic Analysis Techniques

- **Testing Processes**
  - Unit, Integration, System, Acceptance, Regression, Stress
- **Testing Approaches**
  - Black Box versus White Box
- **Black Box Strategies**
  - Test case selection criteria
  - Representations for considering combinations of events/states

# White Box/Structural Test Data Selection

- Coverage based
- Fault-based
  - e.g., mutation testing, RELAY
- Failure-based
  - domain and computation based
  - use representations created by symbolic execution

## Coverage Criteria

- control-flow adequacy criteria
- $G = (N, E, s, f)$  where
  - the nodes  $N$  represent executable instructions (statement or statement fragment)
  - the edges  $E$  represent the potential transfer of control
  - $s \in N$  is a designated start node
  - $f \in N$  is a designated final node
  - $E = \{ (n_i, n_j) \mid \text{syntactically, the execution of } n_j \text{ follows the execution of } n_i \}$

# Control-Flow-Graph-Based Coverage Criteria

- **Statement Coverage**
- **Branch Coverage**
- **Path Coverage**
- **Hidden Paths**
- **Loop Guidelines**
  - **General**
  - **Boundary - Interior**



## Statement Coverage

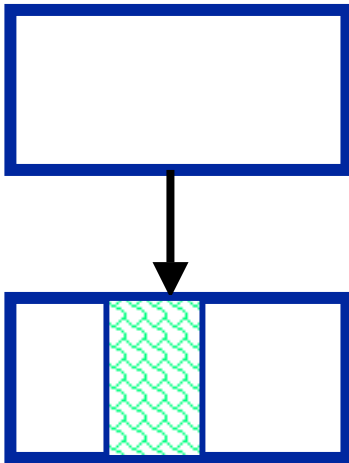
- requires that each statement in a program be executed at least once
- formally:
  - a set  $P$  of paths in the CFG satisfies the statement coverage criterion iff for each  $n_i \in N$ ,  $\exists p \in P$  such that  $n_i$  is on path  $p$ 
    - defined in terms of paths

## Statement Coverage

- only about 1/3 of NASA statements were executed before software was released (Stucki 1973)
- usually can achieve 85% coverage easily, but why not 100%?
  - unreachable code
  - complex sequence (should be tested!)
- Microsoft reports 80-90% code coverage

## How does OO affect coverage?

- Often only parts of a reused component are actually executed by a system
  - Would expect good coverage for unit testing
  - More restricted coverage for integration testing



## Coincidental Correctness

- Executing a statement does not guarantee that a fault on that path will be revealed

- Example:

$Y := X * 2$

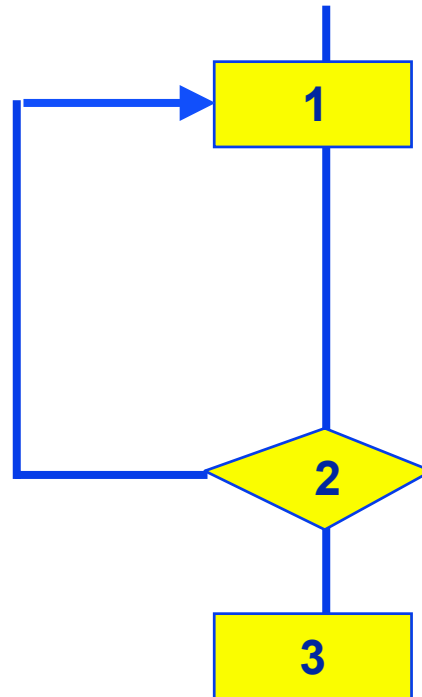
$Y := X * * 2$

If  $x = 2$  then the  
fault is not exposed

## Branch Coverage

- Requires that each branch in a program (each edge in a control flow graph) be executed at least once
  - e.g., Each predicate must evaluate to each of its possible outcomes
- Branch coverage is stronger than statement coverage

# Branch Coverage



**STATEMENT COVERAGE: PATH 1, 2, 3**

**BRANCH COVERAGE: PATH 1, 2, 1, 2, 3**

# Hidden Path (branch) Coverage

- Requires that each condition in a compound predicate be tested

Example:

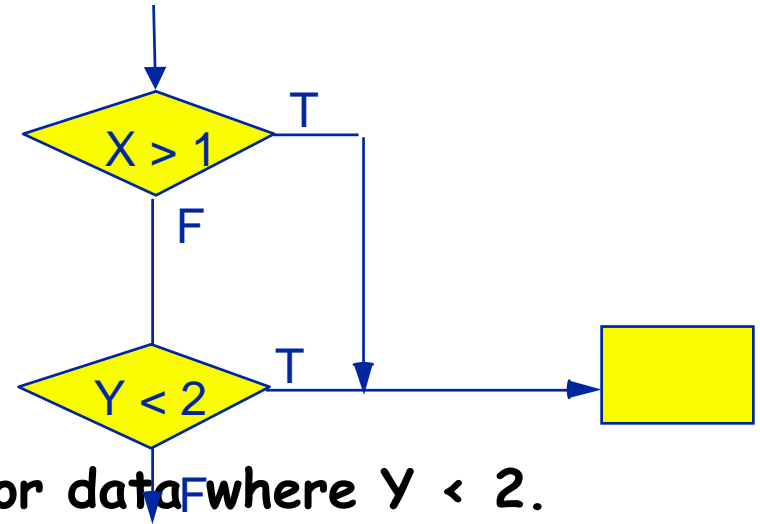
$$(X > 1) \vee (Y < 2)$$

Test Data:

$$X = 2, Y = 5 \rightarrow T$$

$$X = 1, Y = 5 \rightarrow F$$

but, true branch is never tested for data where  $Y < 2$ .



$$\begin{array}{cc} (X > 1) & (Y < 2) \\ T & F \\ F & T \\ T & T \\ F & F \end{array}$$

## Path Coverage

- Requires that every executable path in the program be executed at least once
- In most programs, path coverage is impossible
  - Example:

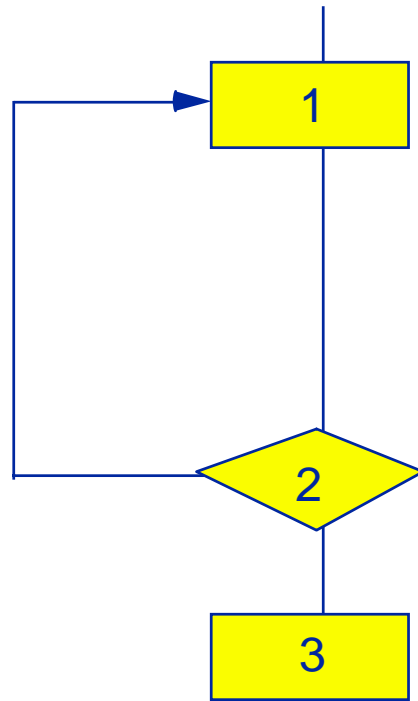
```
read N;  
SUM := 0;  
for I = 1 to N do  
  read X;  
  SUM := SUM + X;  
endfor
```

- How do we choose a set of paths?



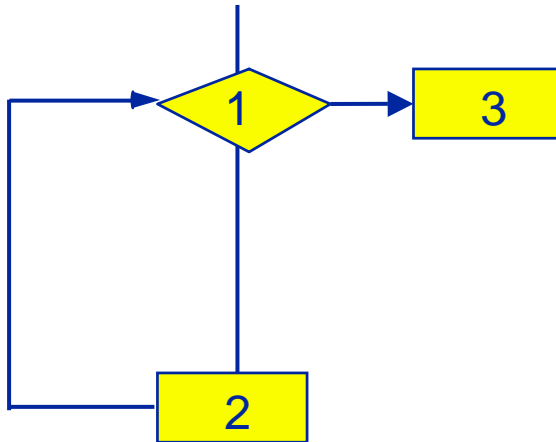
## Loop Coverage

- Path 1, 2, 1, 2, 3 executes all branches (and all statements) but does not execute the loop well.



## Typical Guidelines for loop coverage

- fall through case
- minimum number of iterations
- minimum +1 number of iterations
- maximum number of iterations



1, 3

1,2,3

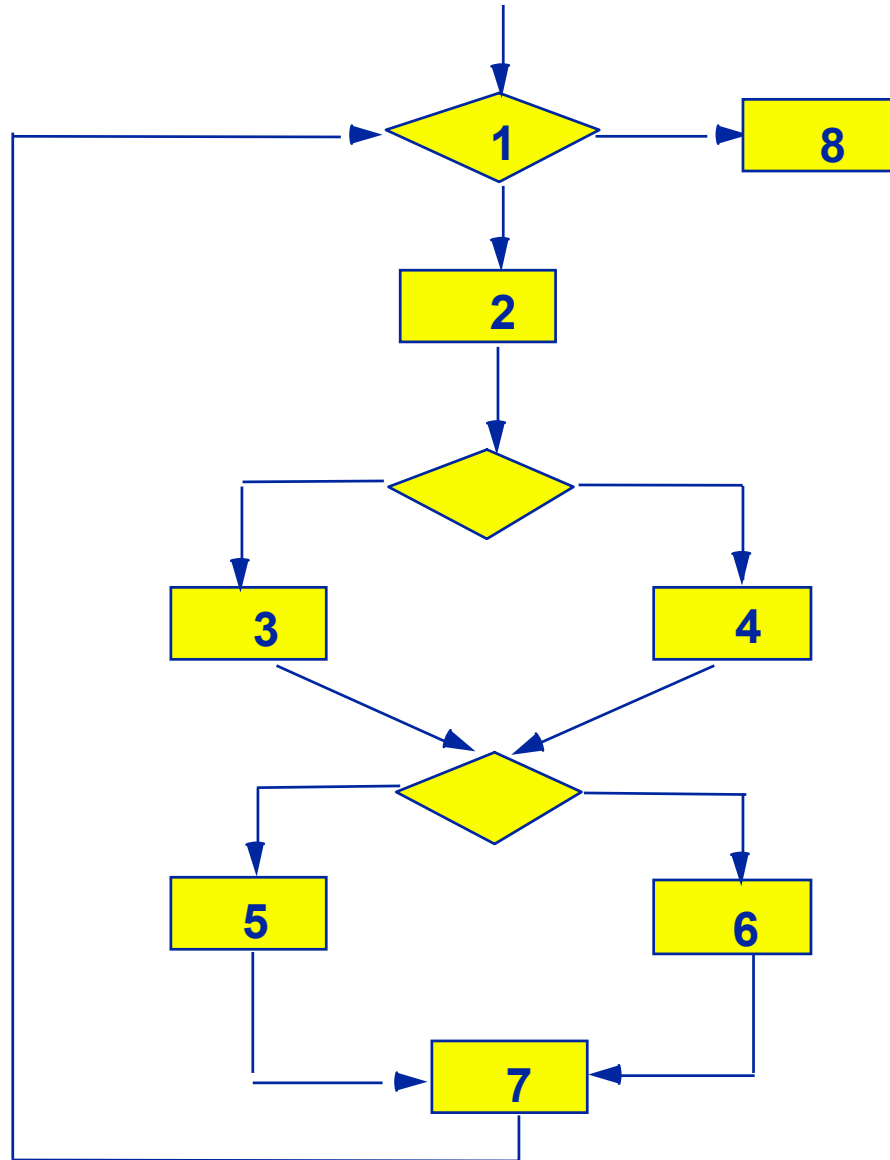
1,2,1,2,3

(1, 2,)<sup>n</sup> 3

## Boundary - Interior Criteria

- **boundary test** of a loop causes the loop to be entered but not iterated
- **interior test** of a loop causes a loop to be entered and then iterated at least once
- both boundary and interior tests are to be selected for each unique path through the the loop

# Example



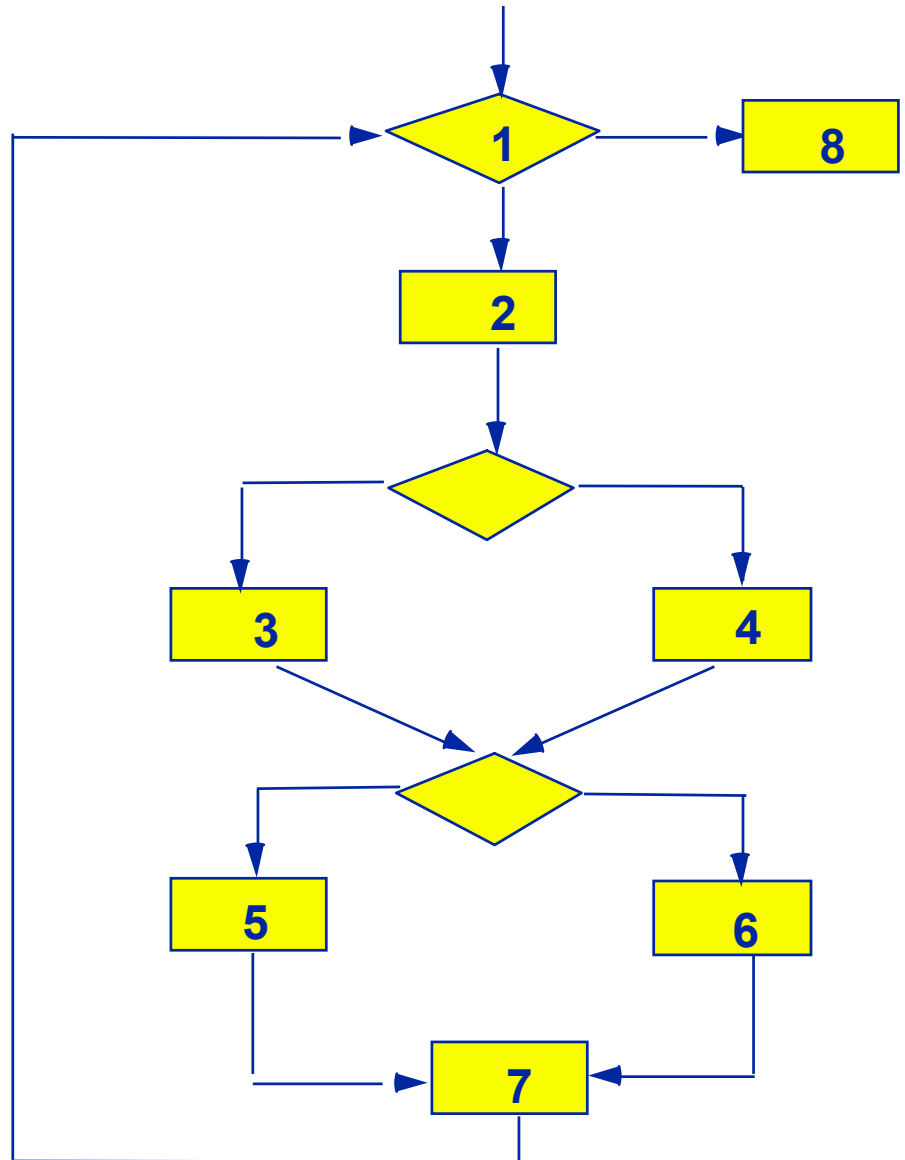
# Paths for Example

## Boundary paths

1,2,3,5,7	a
1,2,3,6,7	b
1,2,4,5,7	c
1,2,4,6,7	d

## Interior paths (for 2 executions of the loop)

a,a  
a,b  
a,c  
a,d  
b,a  
b,b  
...  
x,y for x,y = a, b, c, d



## Selecting paths that satisfy these criteria

- **static selection**
  - some of the associated paths may be infeasible
- **dynamic selection**
  - monitors coverage and displays areas that have not been satisfactorily covered

## Problem with coverage criteria:

- Fault detection may depend upon
  - Specific combinations of statements, not just coverage of those statements
  - Astutely selected test data that reveals the fault, not just test data that executes the statement/branch/path
- Will look at semantically richer models
- First look at some axioms about testing criteria

# Axiomatizing Software Test Data Adequacy

- Elaine Weyuker, Dec. 86, TSE
- Adequacy criteria for testing determines whether it is reasonable to stop testing
- Axioms are basic assumption that “well formed” criteria should satisfy
- A system that executes a test set T that satisfies an adequacy criterion is **NOT** necessarily correct
  - Correctness would be too strong
  - Only exhaustive testing would satisfy correctness



## Weyuker's axioms

- for every system there exists an adequate test set [**ADEQUACY**]
  - Assuming that a system's domain is always finite, then the adequate test set is finite
- There is a system  $S$  and a test set  $T$  such that  $S$  is adequately tested by  $T$ , and  $T$  is not an exhaustive test set [**NON-EXHAUSTIVE APPLICABILITY**]
- If  $T$  is adequate for  $S$  and  $T$  is a subset of  $T'$ , then  $T'$  is adequate for  $S$  [**MONOTONICITY**]

## Weyuker's axioms

- the empty set is not adequate for any system [INADEQUATE EMPTY SET]
- let  $S$  be a renaming of  $Q$ , then  $T$  is adequate for  $S$  if and only if  $T$  is adequate for  $Q$  [RENAMING]
  - Superficial change does not change test cases

## Weyuker's axioms

- if two systems compute the same function, a test set that is adequate for one is not necessarily adequate for the other  
[ANTI-EXTENSIONALITY]
  - Semantic equivalence does not preserve testing criteria
  - Implies that implementation must be taken into consideration
- if two systems are the same shape, a test set that is adequate for one is not necessarily adequate for the other [GENERAL MULTIPLE CHANGE]
  - Same shape means same CFG and same variables are referenced and defined at the nodes
  - Same values may not be computed

## Weyuker's axioms

- for every  $n$ , there is a system  $S$  such that  $S$  is adequately tested by a set of size  $n$ , but not by any test set of size  $n-1$

[COMPLEXITY]

- Need at least  $n$  test cases
- Any  $n$  test cases may not be adequate, however

## Weyuker's axioms

- there exists a system  $S$  with a subcomponent  $Q$  such that  $T$  is adequate for  $S$ ,  $T'$  is the set of vectors of values that variables can assume on entrance to  $Q$  and  $T'$  is not adequate for  $Q$

### [ANTI-DECOMPOSITION]

- $S$  constrains the values that can be applied to  $Q$  and thus does not adequately test  $Q$

## Are these axioms?

- A principle that is accepted as true without proof as the basis for argument; a postulate  
(The American Heritage® Dictionary of the English Language, Third Edition copyright © 1992 by Houghton Mifflin Company. Electronic version licensed from InfoSoft International, Inc. All rights reserved)
- Want a set of axioms that are consistent and lead to theorems that provide insight
- Weyuker's "axioms" are not axioms, but desired properties
  - Showed that most testing criteria do NOT satisfy all these "axioms"

## Stopping rule vs. Measurement

- $C:(S,T) \rightarrow \{true, false\}$       **stopping rule**
- $C: (S,T) \rightarrow [0,1]$       **measurement**

## Zhu and Hall's Measurement Theory

- For all systems  $S$  and specifications  $R$ ,
  - the adequacy of the empty test is 0
  - the adequacy of exhaustive testing is 1
  - If test set  $t_1$  is a subset of test set  $t_2$ , then the adequacy of  $t_1$  is less than or equal to the adequacy  $t_2$  (monotonicity)